

# Product Differentiation and Oligopoly: a Network Approach

Bruno Pellegrino

University of Maryland



**Autoridade da Concorrência**  
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# Research Question

- **Motivation:** large dispersion in markups across firms
  - ▶ Rising level & dispersion (De Loecker, Eeckhout & Unger, 2020)
  - ▶ Rising industry concentration (Kwon et al. 2022)
- **Research Question:** what's behind this heterogeneity? What's driving these trends? What are the welfare implications?
  - ▶ Consumer surplus and deadweight loss **due to oligopoly**
- **Challenge:** IO question in a macroeconomic setting:
  - ▶ Standard IO tools are not available (scalability, lack of data)
  - ▶ No systematic, objective way to define product markets.

# This Paper

- **Methodological contribution:** bring IO in macroeconomics.
- **Theory of oligopoly and markups in general equilibrium**
  - ▶ Forget about industries: in this model, oligopolistic firms compete in a network of product market rivalries.
  - ▶ New demand system: Generalized Hedonic-Linear (GHL).
- **Taken to the data** (and validated) for universe of US public firms, using product similarity data by **Hoberg & Phillips (2016)**.
- **Decompose markups** into 2 forces: productivity and centrality.
- **Welfare measurement:** large, increasing oligopoly deadweight loss (12.7% of total surplus in 2019), major distributional effects.

# Literature

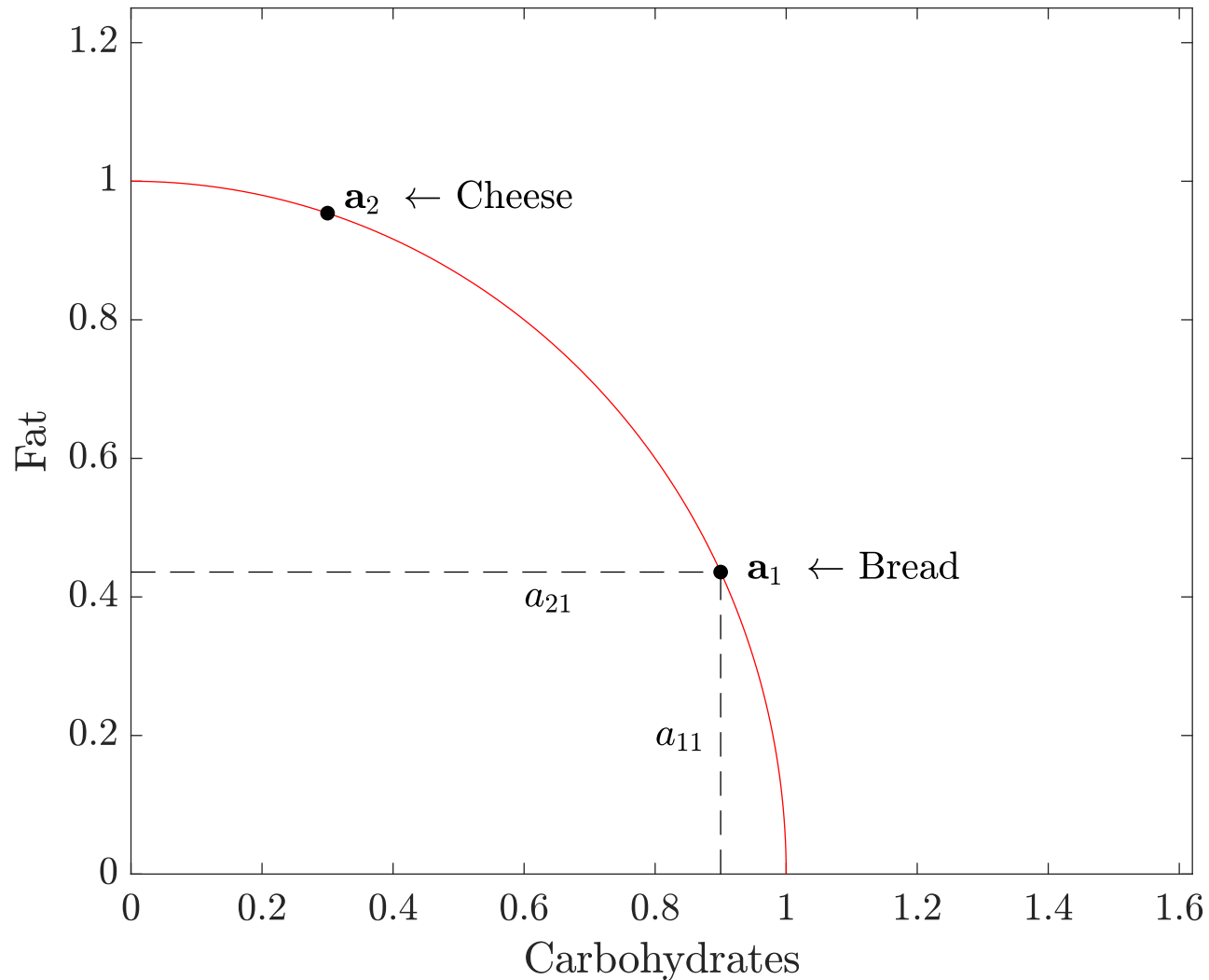
- **Rising Markups and Industry Concentration:** De Loecker, Eeckhout & Unger (2020), Grullon, Larkin & Michaely (2019); Kwon, Ma & Zimmermann (2021), Eeckhout & Veldkamp (2022).
- **Distortions, Input/Output, Micro Origins of Aggregate TFP:** Gabaix (2011); Acemoglu, Carvalho, Ozdaglar, Tahbaz-Salehi (2012); Baqaee & Farhi (2020); Bigio & La'O (2020); Edmond, Midrigan & Xu (2019); Carvalho, Elliot & Spray (2022);
- **Hedonic Demand/Empirical IO:** Lancaster (1968); Rosen (1974); Epple (1987) Berry, Levinsohn & Pakes (1994); Nevo (2001)...
- **Network Games:** Ballester, Calvo-Armengol & Zenou (2006); Galeotti, Golub, Goyal, Talamer & Tamuz (2022).
- **Text Analysis/Product Similarity:** Hoberg & Phillips (2016).

# Theory

# Generalized Hedonic-Linear Demand

- $i = 1, 2, \dots, n$  firms that behave as oligopolists.
- **Hedonic demand:** each firm's product is a bundle of characteristics (Lancaster, 1968; Rosen, 1974; Epple, 1987, Berry, Levinsohn & Pakes 1994; etc.)
- 1 unit of product  $i$  provides:
  - ▶ 1 unit of an idiosyncratic characteristic  $i$
  - ▶ a vector of  $k$  common characteristics  $\mathbf{a}_i$  (length 1)

# A basic example: 2 firms, 2 characteristics



# Aggregating common characteristics

**Characteristics**  
(Nutrient Intake)

**Matrix of Coordinates**  
(Nutrition Facts)

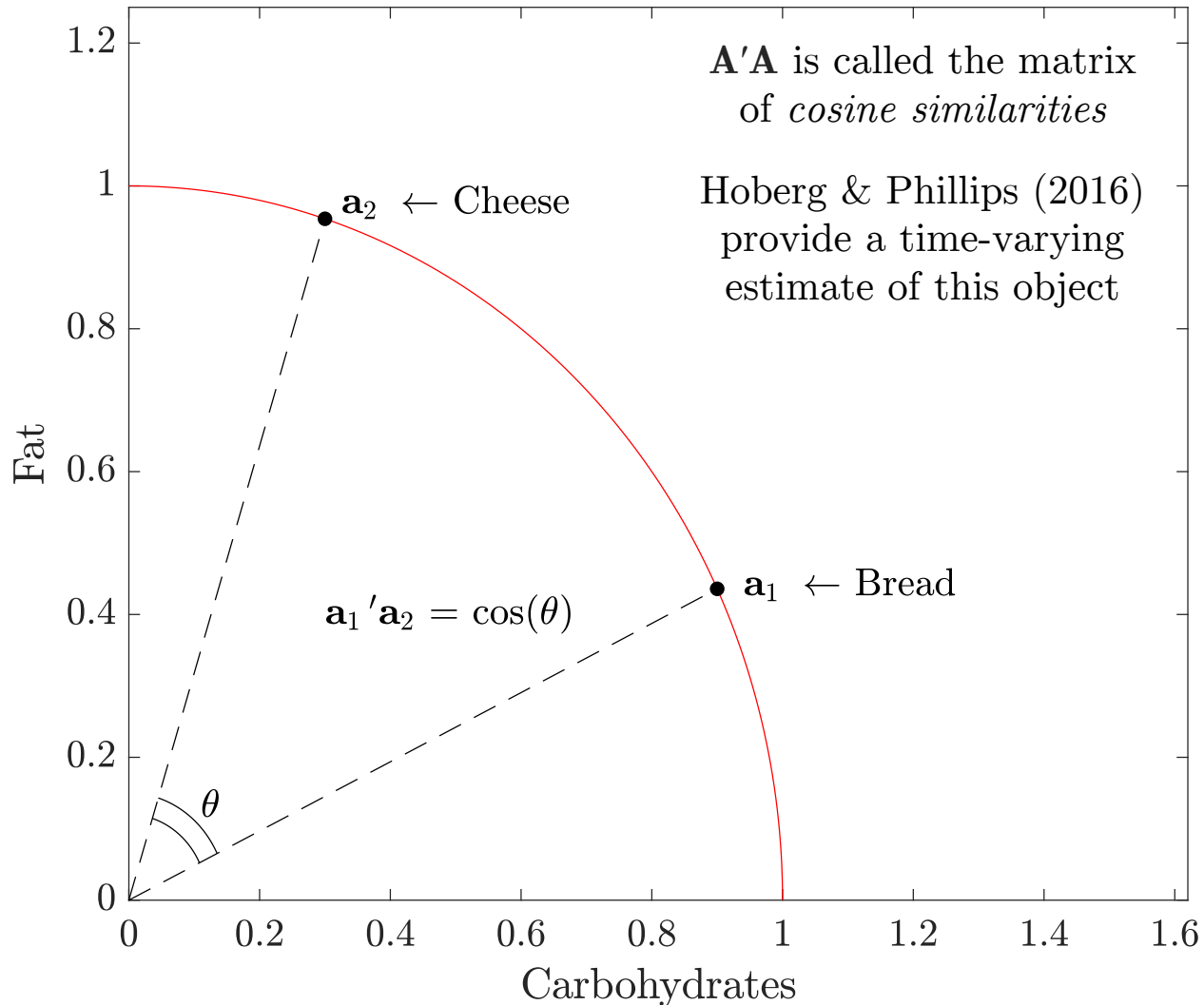
**Product**  
**Bundle**

$$\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_k \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{k1} & a_{k2} & \cdots & a_{kn} \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \\ \vdots \\ q_n \end{bmatrix}$$

$$\mathbf{x} = \mathbf{A}\mathbf{q}$$



# Defining Cosine Similarity



# Representative Consumer-Worker-Investor

- Quadratic utility  $U(\mathbf{x}, \mathbf{y}, H) =$

$$\alpha \cdot \sum_{k=1}^m \left( b_k^x x_k - \frac{1}{2} x_k^2 \right) + (1 - \alpha) \sum_{i=1}^n \left( b_i^y y_i - \frac{1}{2} y_i^2 \right) - H$$

- $H =$  hours worked – numeraire
- Consumer faces vector of prices  $\mathbf{p}$  and chooses demand  $\mathbf{q}$ , subject to profits and labor income being  $\geq \mathbf{p}'\mathbf{q}$ .

# Inverse Demand

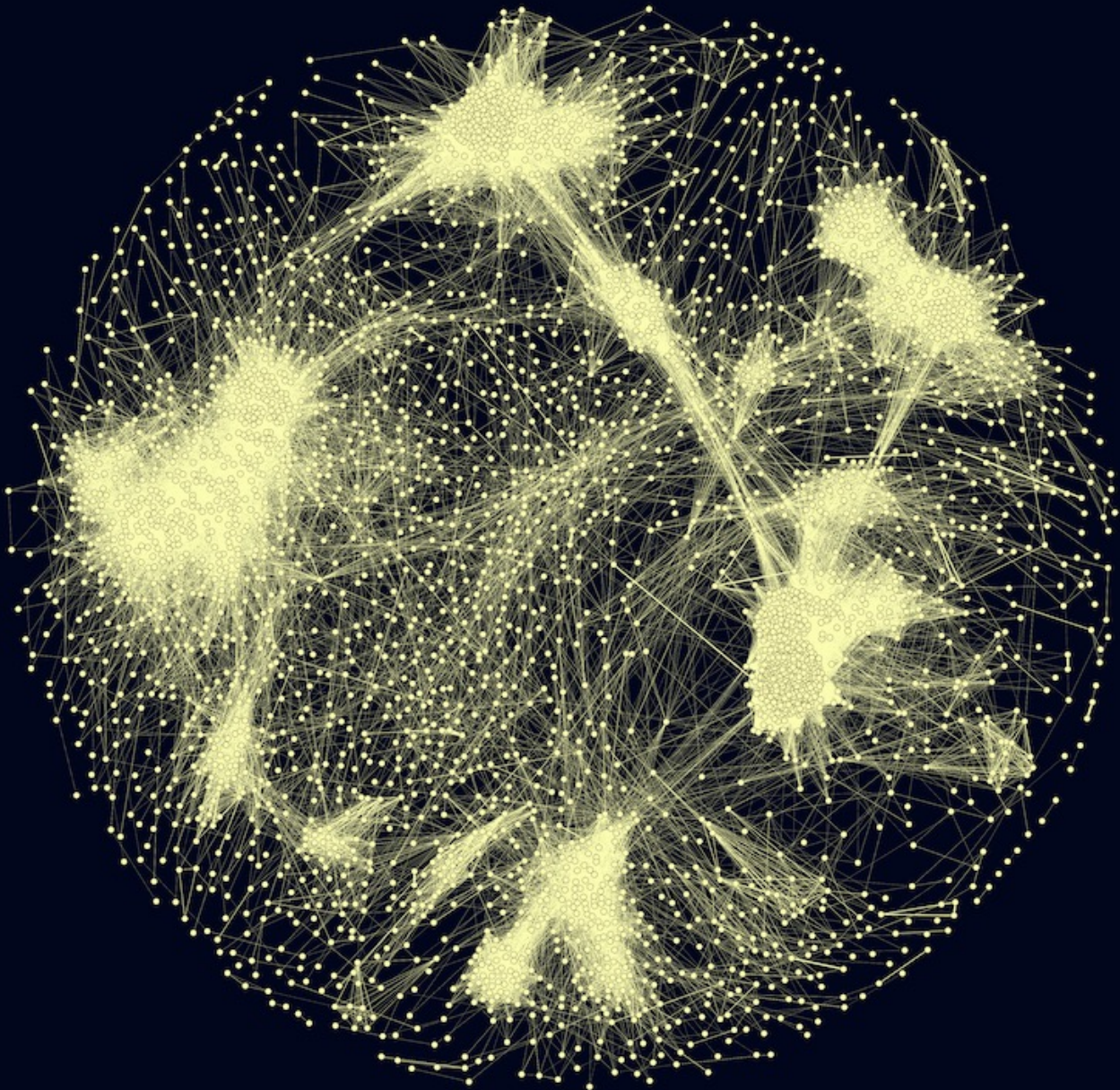
$$\mathbf{p} = \mathbf{b} - (\mathbf{I} + \mathbf{\Sigma}) \mathbf{q}$$

where

$$\mathbf{\Sigma} \stackrel{\text{def}}{=} \alpha (\mathbf{A}'\mathbf{A} - \mathbf{I})$$

# Cost Function and Competition

- Cost function (can be relaxed):  $h_i = f_i + c_i^0 q_i + \frac{1}{2} \delta_i q_i^2$
- Cournot Competition: firm  $i$  chooses supply  $q_i$  to maximize profits function  $\pi_i$  (also quadratic)
- (Linear-quadratic) Network game
  - ▶ Ballester, Calvó-Armengol & Zenou, 2006
- Why? the matrix of cosine similarities  $\mathbf{A}'\mathbf{A}$  (proportional to  $\mathbf{\Sigma}$ ) can be thought of as an adjacency matrix of a network



# Cournot-Nash Equilibrium

$$\mathbf{q} = (2\mathbf{I} + \Delta + \Sigma)^{-1} (\mathbf{b} - \mathbf{c}^0)$$

Scale Economies      Network Position      Marginal Surplus at  $q_i = 0$

The expression above can be shown to be a measure of network centrality (Katz-Bonacich)

# Hedonic-Adjusted Productivity

$$\omega_i \stackrel{\text{def}}{=} \frac{b_i}{c_i}$$

- Accounts for product quality
- Volumetric-invariant
- Comparable across widely-different firms

# Decomposing Markups

**Monopolistic Markup**

$$= (1 + \omega_i)/2$$



$$\mu_i = \chi_i + (1 - \chi_i) \bar{\mu}_i$$



**Product Market Centrality**

Depends on the entire matrix of cosine similarities  $\mathbf{A}'\mathbf{A}$ . The profit share of surplus is a decreasing function of  $\chi_i$  alone



# Data and Validation

# Hoberg & Phillips (2016 JPE) Product Similarity

- By law, every public corporation in the US has to file SEC form 10-K on a yearly basis.
- First 6-10 pages contain the “Business Description”.
- HP created time-varying measures of cosine similarity between firms by text-mining these business descriptions.
- Solve long-standing problems with NAICS/SIC: static, binary do not reflect product market competition, can be manipulated.
- Highly incentive compatible - standard in finance: use of NAICS and SIC is no longer considered acceptable to capture product market rivalries, at least for top finance journals.

# Construction

$$\mathbf{v}_i = \begin{bmatrix} v_{i,1} \\ v_{i,2} \\ \vdots \\ v_{i,61146} \end{bmatrix} \quad \cos_{ij}^{\text{HP}} \stackrel{\text{def}}{=} \frac{\mathbf{v}'_i \mathbf{v}_j}{\sqrt{\|\mathbf{v}_i\| \|\mathbf{v}_j\|}}$$

**Identification:** bijective mapping words  $\Leftrightarrow$  characteristics,  
 $\mathbf{a}_i$  and  $\mathbf{v}_i$  are collinear up to permutation  $\Rightarrow \mathbf{a}'_i \mathbf{a}_j \equiv \cos_{ij}^{\text{HP}}$

# Identification

- Compustat: Revenues ( $p_i q_i$ ), COGS ( $TVC_i$ ), SG&A ( $f_i$ ).
- Assume  $\delta_i=0$  (later relaxed). Only one free parameter:  $\alpha$ .
- **Proposition:**  $\partial \log p_i / \partial \log q_j$  is observed for firm pair (K,Q):

$$\alpha = - \frac{\varepsilon_{KQ} \cdot p_K q_K + \varepsilon_{QK} \cdot p_Q q_Q}{2 \cdot \cos_{KQ}^{HP} \cdot \sqrt{p_K q_K - TVC_K} \cdot \sqrt{p_Q q_Q - TVC_Q}}$$

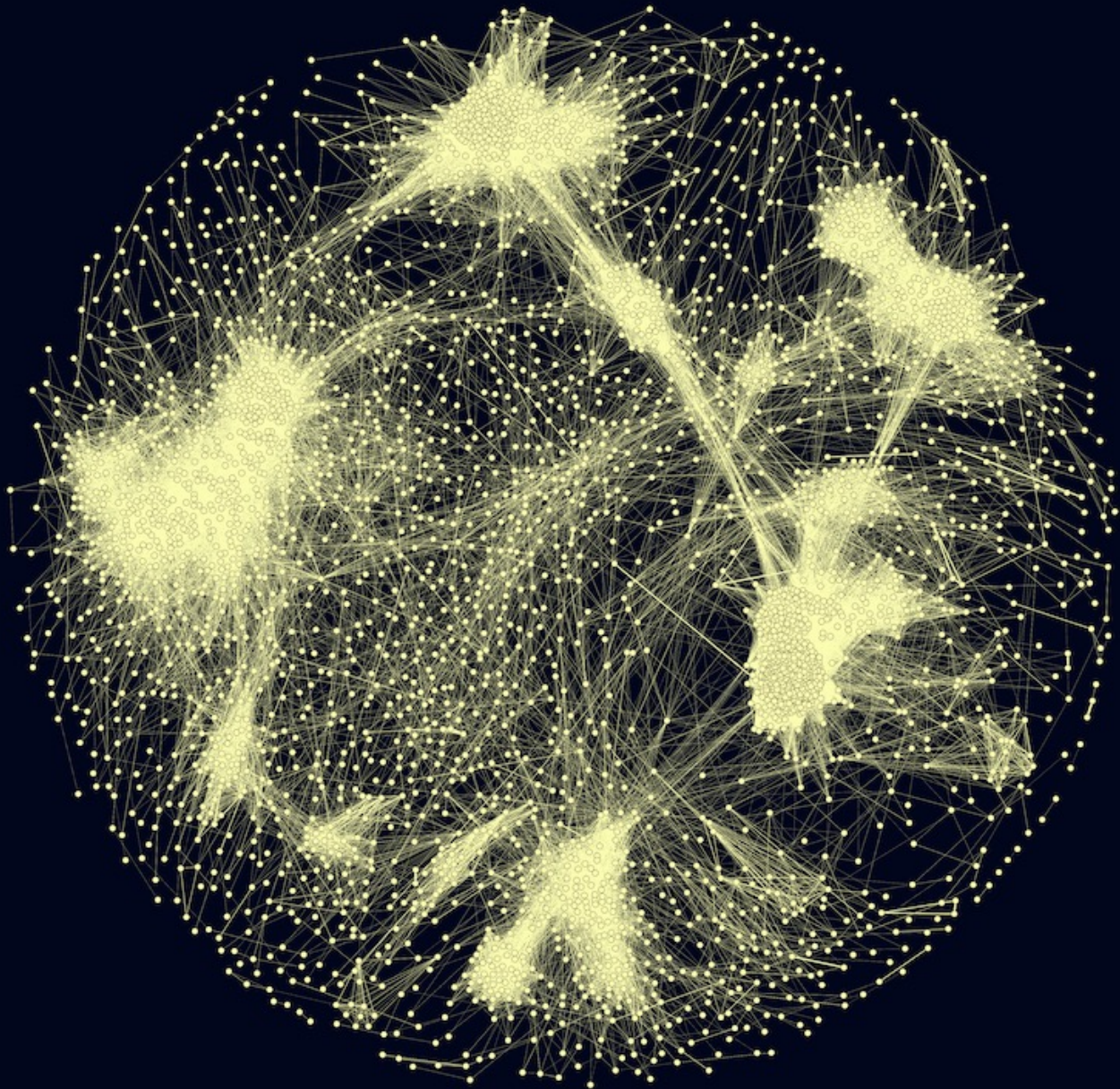
- Every other object is identified in closed form (correct units).

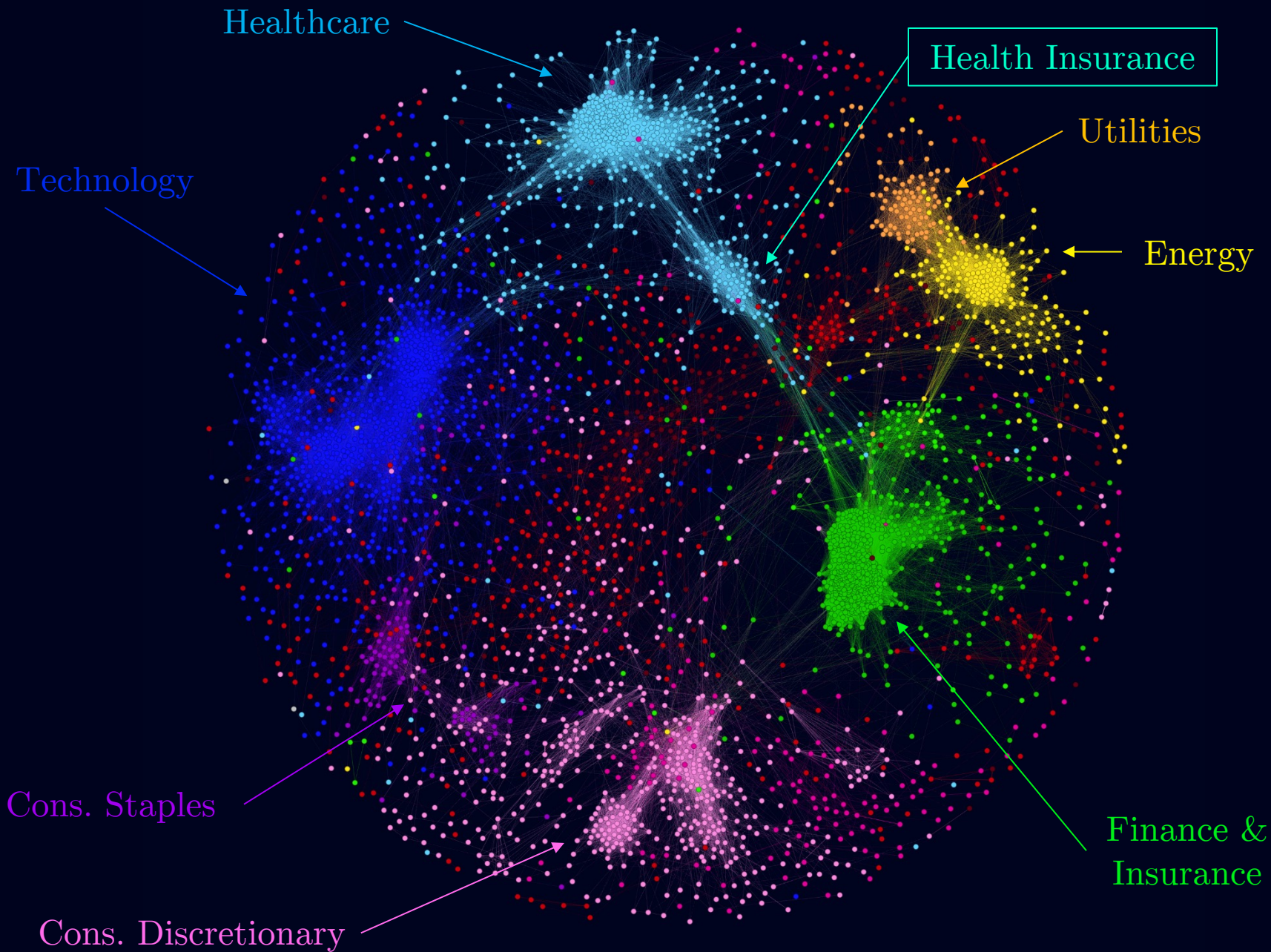
# Identification

$$q_i = \sqrt{\pi_i}$$

$$c_i = \frac{\text{TVC}_i}{q_i}$$

$$\mathbf{b} = (2\mathbf{I} + \mathbf{\Sigma}) \mathbf{q} + \mathbf{c}$$

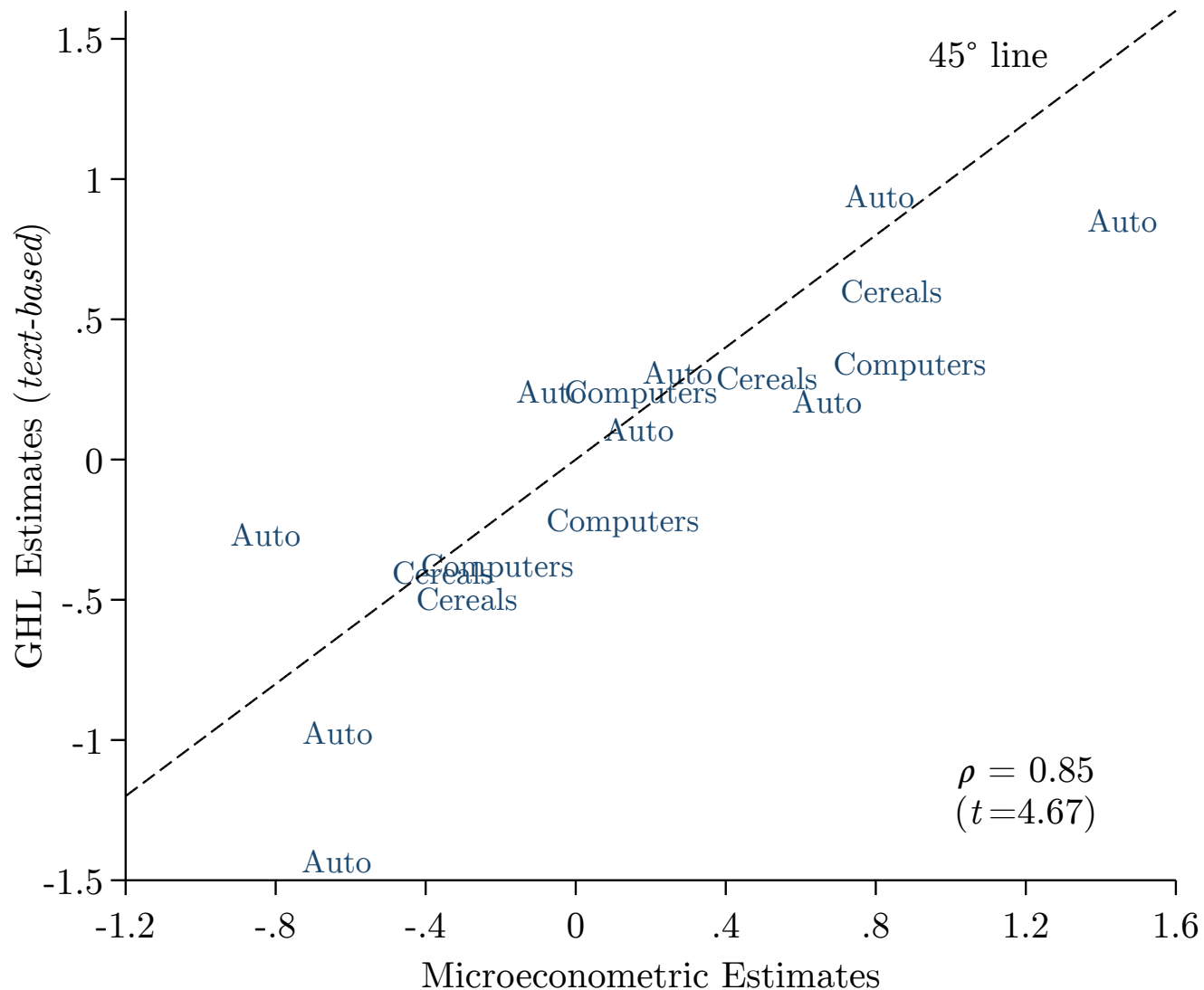




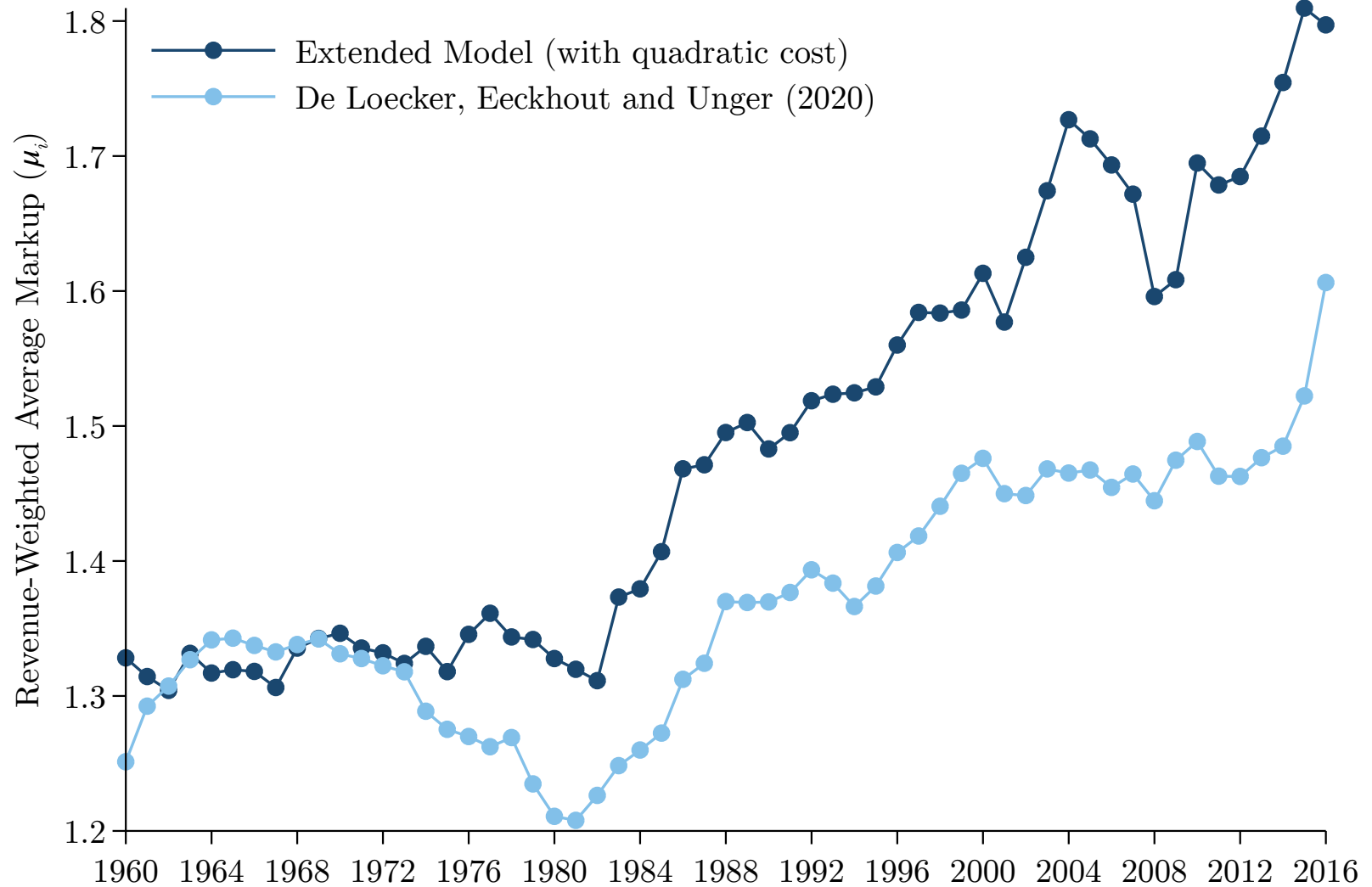
<b>Market</b>	<b>Firm <math>i</math></b>	<b>Firm <math>j</math></b>	<b>Micro Estimate</b>	<b>GHL (<i>text-based</i>)</b>
Auto	Ford	Ford	-4.320	-5.197
Auto	Ford	General Motors	0.034	0.056
Auto	Ford	Toyota	0.007	0.017
Auto	General Motors	Ford	0.065	0.052
Auto	General Motors	General Motors	-6.433	-4.685
Auto	General Motors	Toyota	0.008	0.005
Auto	Toyota	Ford	0.018	0.025
Auto	Toyota	General Motors	0.008	0.008
Auto	Toyota	Toyota	-3.085	-4.851
Cereals	Kellogg's	Kellogg's	-3.231	-1.770
Cereals	Kellogg's	Quaker Oats	0.033	0.023
Cereals	Quaker Oats	Kellogg's	0.046	0.031
Cereals	Quaker Oats	Quaker Oats	-3.031	-1.941
Computers	Apple	Apple	-11.979	-8.945
Computers	Apple	Dell	0.018	0.025
Computers	Dell	Apple	0.027	0.047
Computers	Dell	Dell	-5.570	-5.110



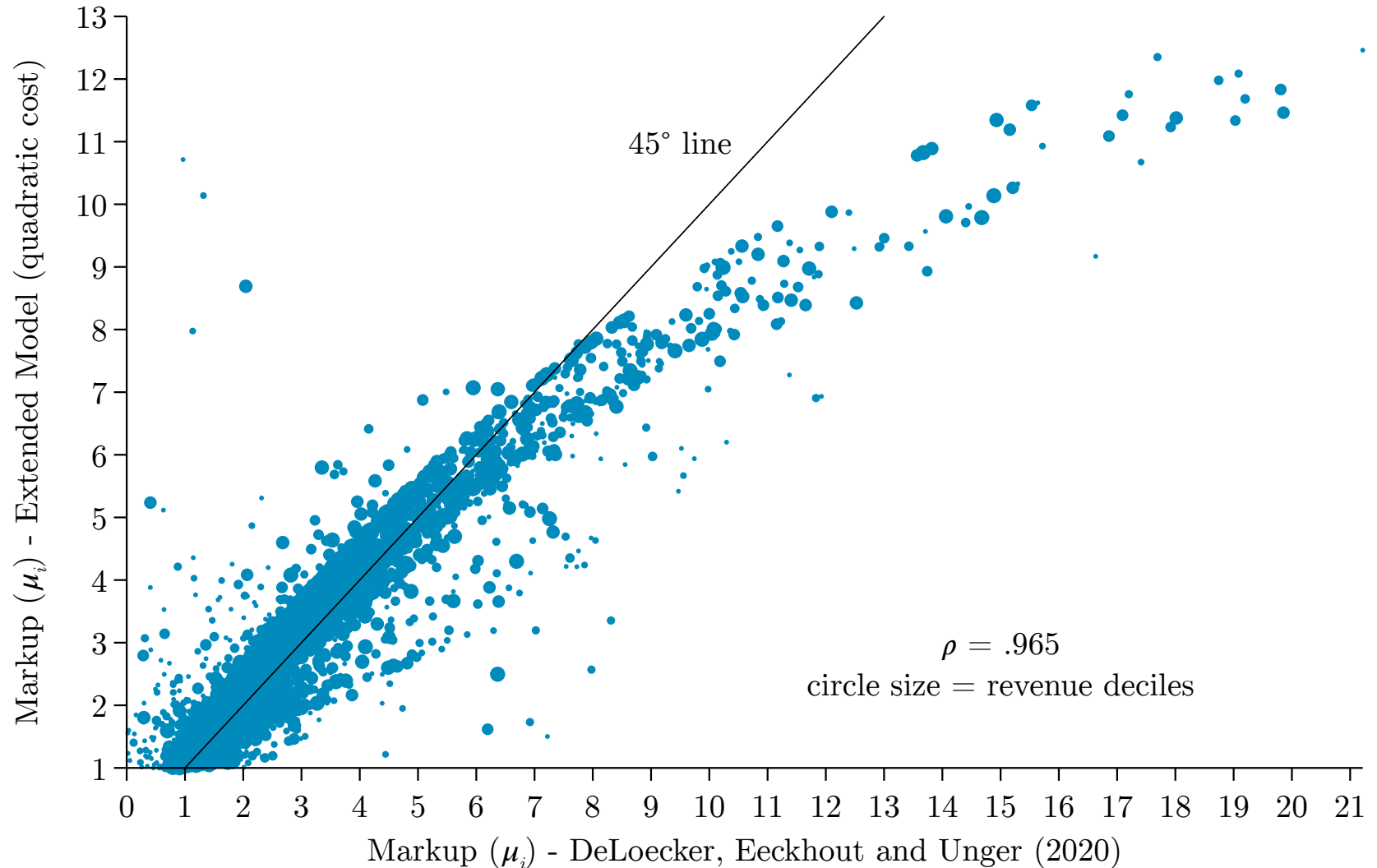
Variable:  $\log \left| \frac{\partial q_i}{\partial p_j} \cdot \frac{p_j}{q_i} \right|$ , residualized on  $(i = j)$  dummy and Market Fixed Effects



# Markups: Time Series

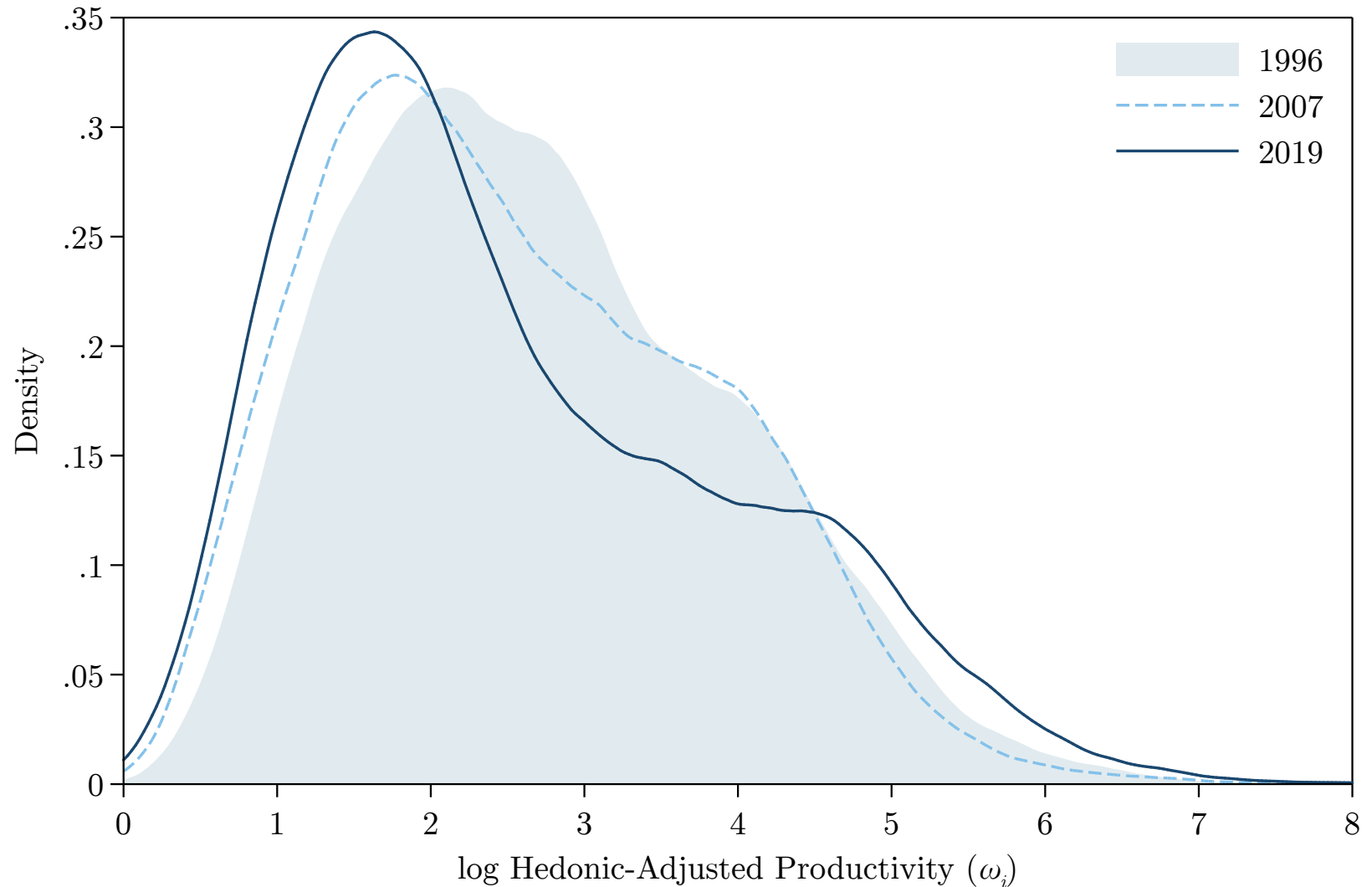


# Markups: Cross-Section

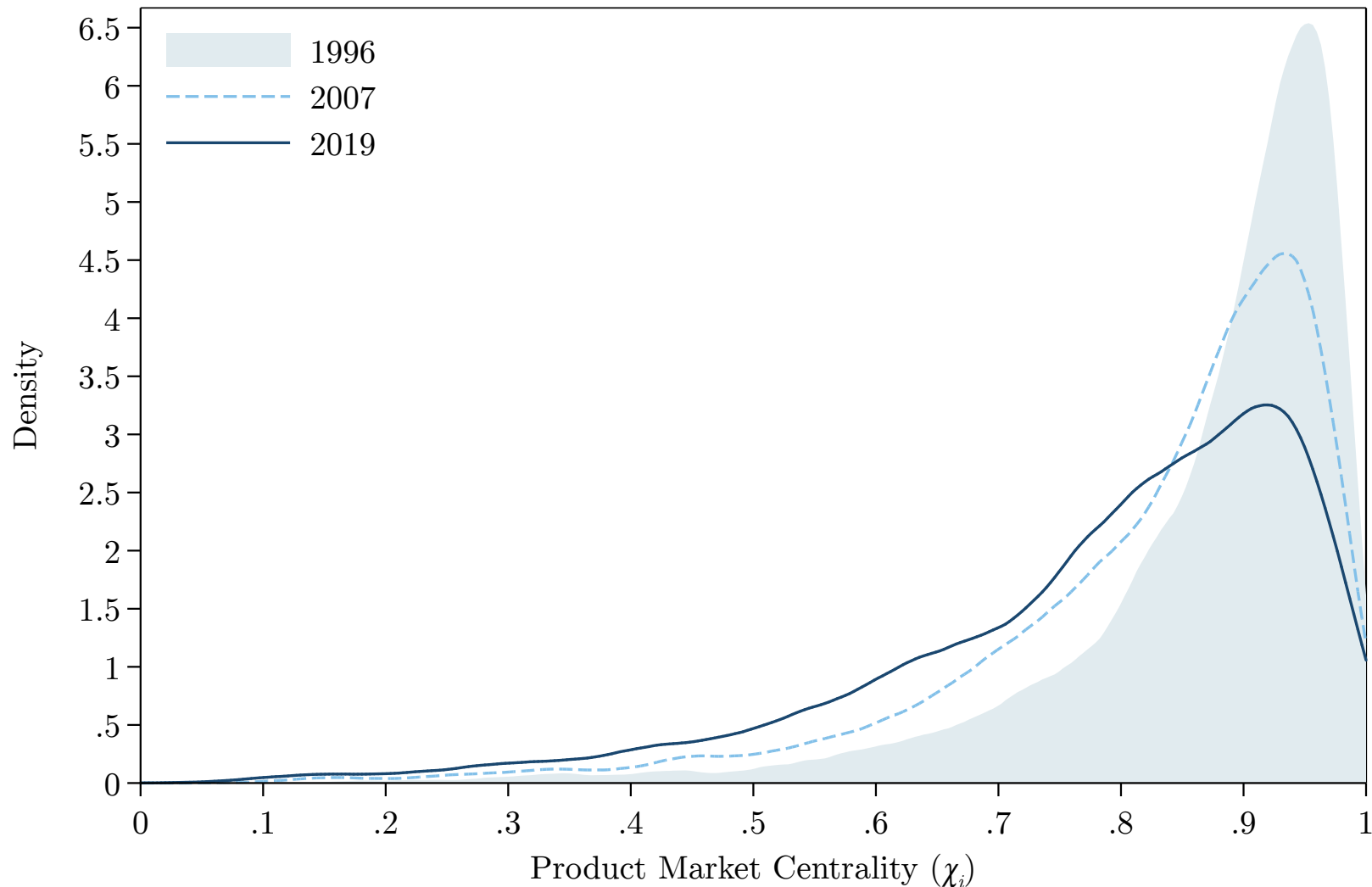


# Empirics

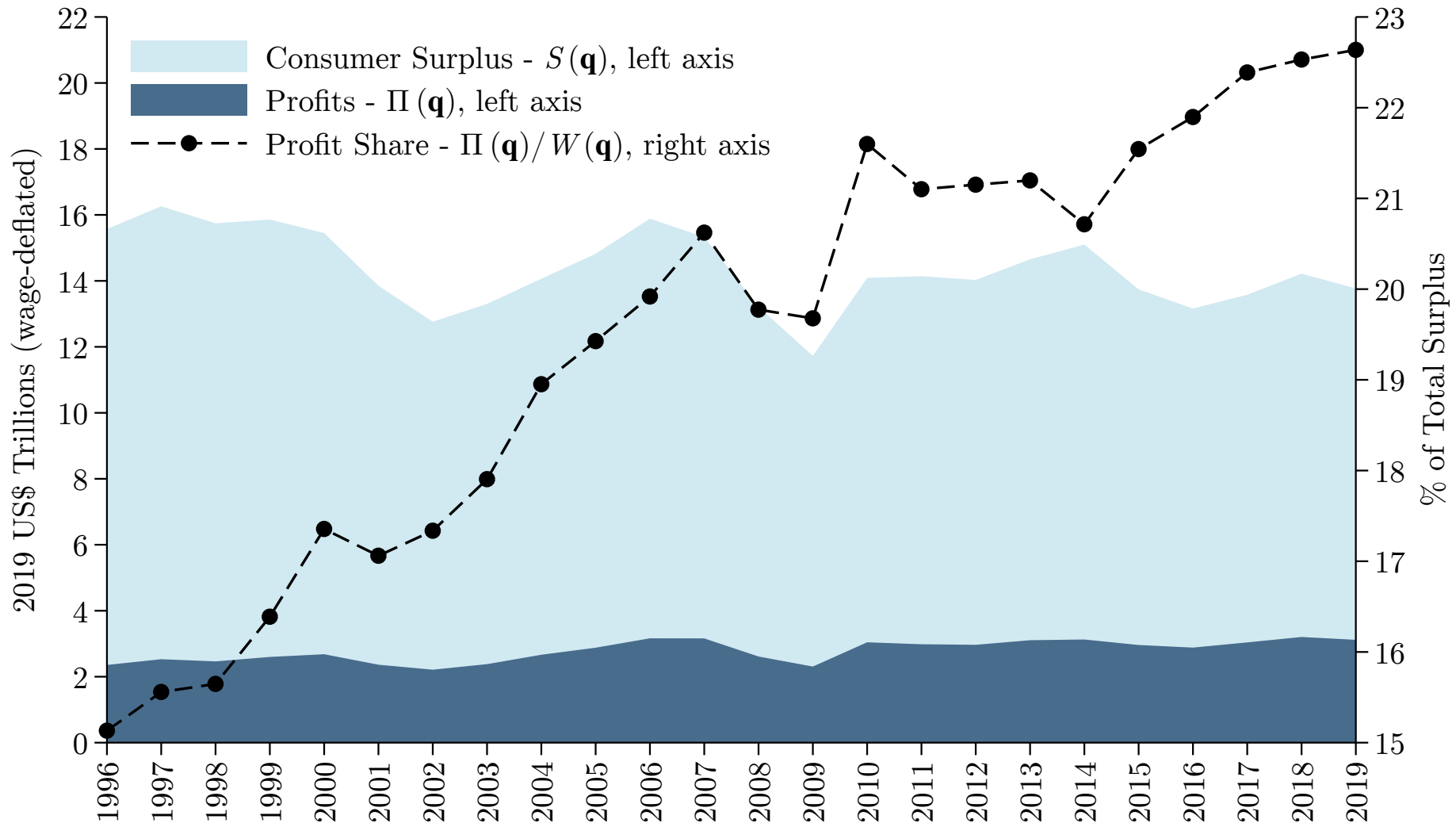
# Distribution of Hedonic-Adjusted Productivity



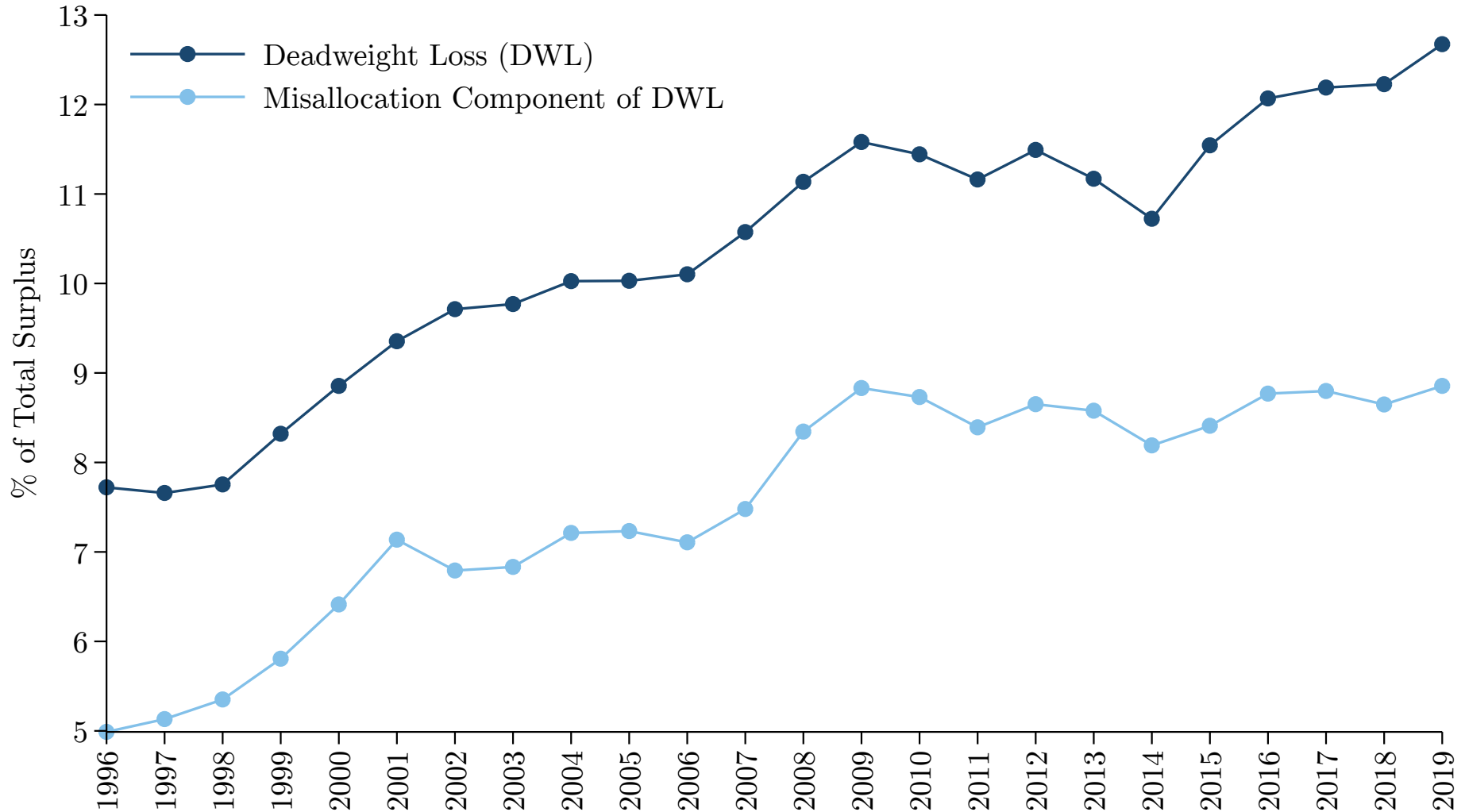
# Distribution of Product Market Centrality



# Total Surplus and its Distribution



# Deadweight Loss from Oligopoly





# Robustness & Extensions

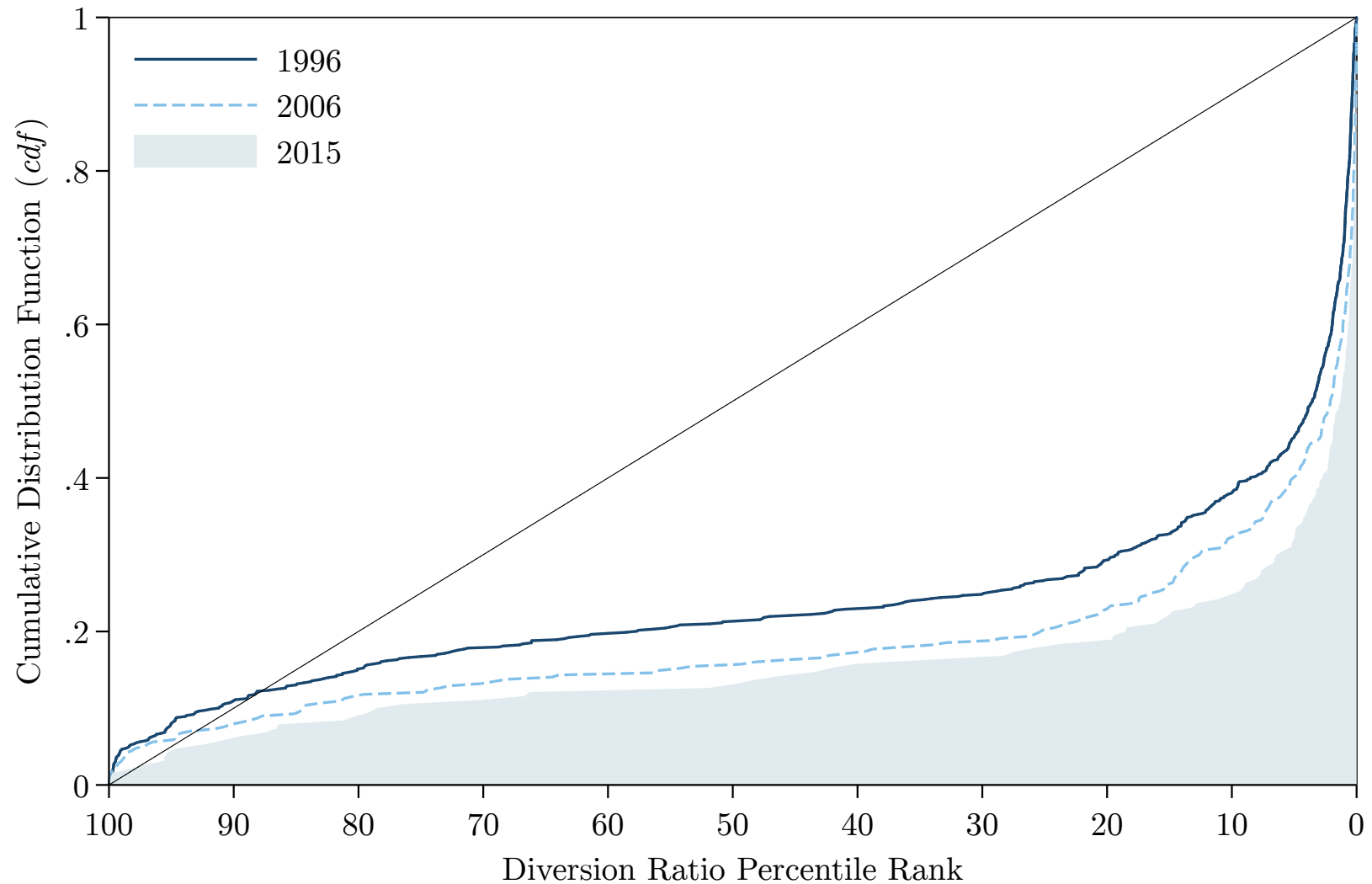
- Private and foreign firms, entry and exit
  - ▶ Aggregation result: add competitive fringes of atomistic firms in the form of a representative firms.
  - ▶ Can be located using firm-sector similarity from FHP.
- Non-flat marginal cost
- Exclude “non-tradable” industries
- Bertrand
- Multi-product firms (using Compustat Segments)
- Input-Output Linkages (using Atalay et al. 2011 IO data)

# Diversion Ratio

To evaluate a merger's anti-competitive potential, the FTC-DOJ merger guidelines recommend looking at Diversion Ratios:

$$\text{Diversion Ratio}_{ij} \stackrel{\text{def}}{=} \frac{\partial q_i}{\partial p_j} \left( \frac{\partial q_j}{\partial p_j} \right)^{-1} = \frac{(\mathbf{I} + \boldsymbol{\Sigma})_{ij}^{-1}}{(\mathbf{I} + \boldsymbol{\Sigma})_{jj}^{-1}}$$

# M&A Activity: Diversion Ratios



# Take-aways

- A new GE theory of oligopoly with hedonic demand.
- Estimated for Compustat using 10-K product similarities.
- Distribution of markups is jointly determined by productivity and product market centrality.
  - ▶ Both have undergone significant changes
- Rising Oligopoly Power
  - ▶ increasing deadweight loss
  - ▶ lower consumer surplus share.
- 👉 I share the data! (elasticities, centrality, productivity...)

# The Great Startup Sellout and the Rise of Oligopoly

Florian Ederer

Yale SOM

Bruno Pellegrino

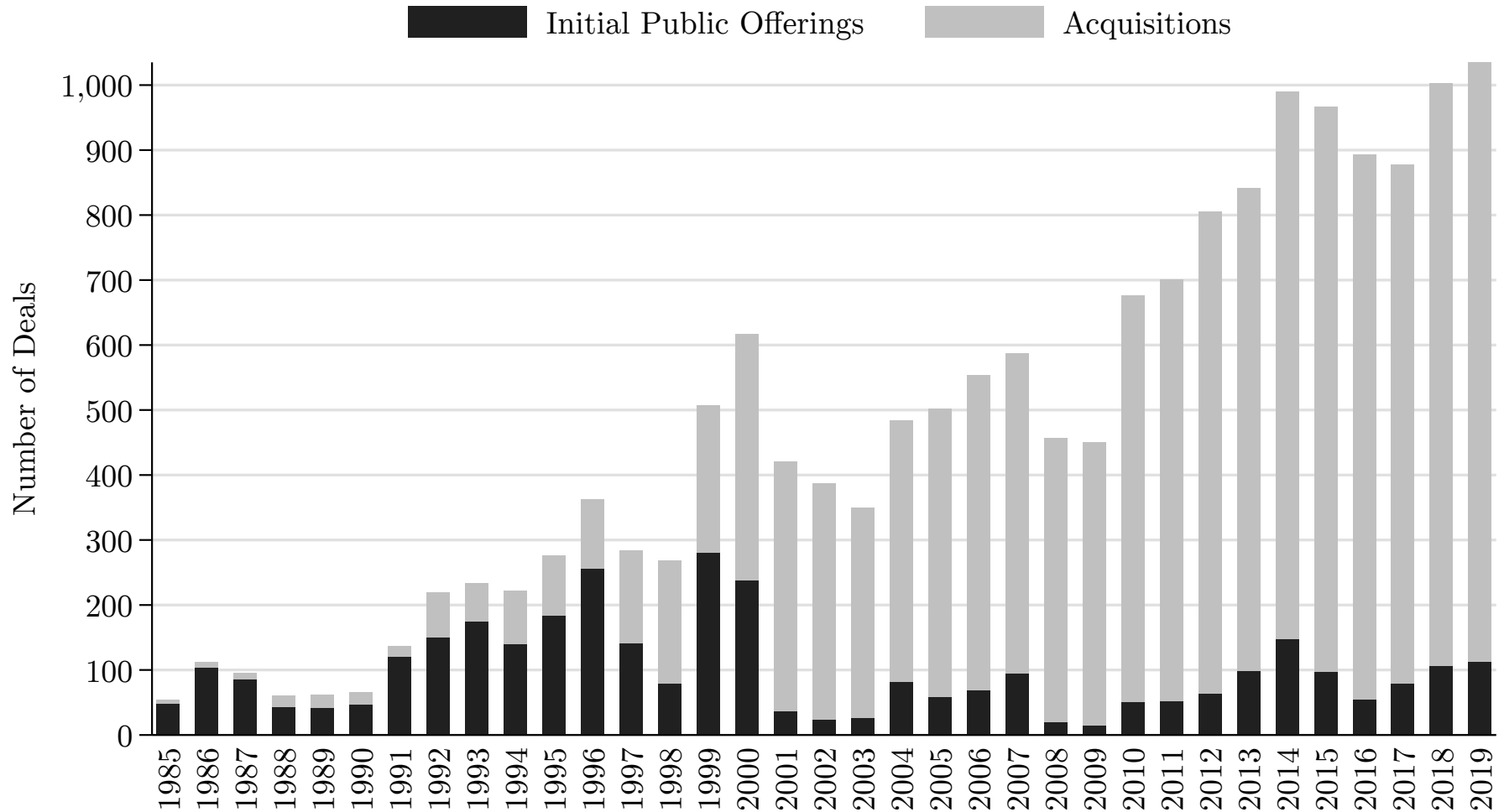
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What is driving the  
increase in oligopoly?

# VC-backed startup exits (1985-2019)

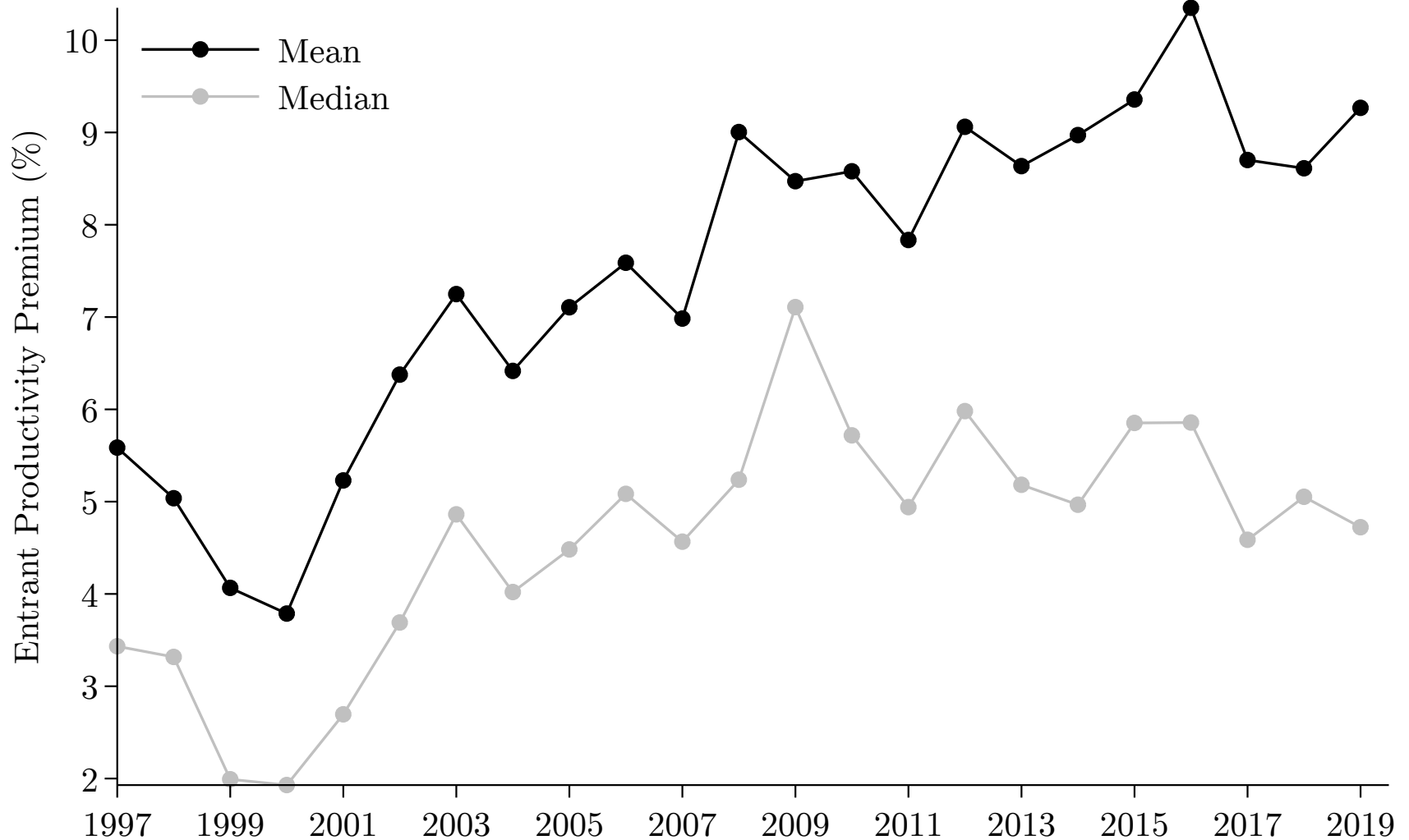


# Entrant Productivity Premium

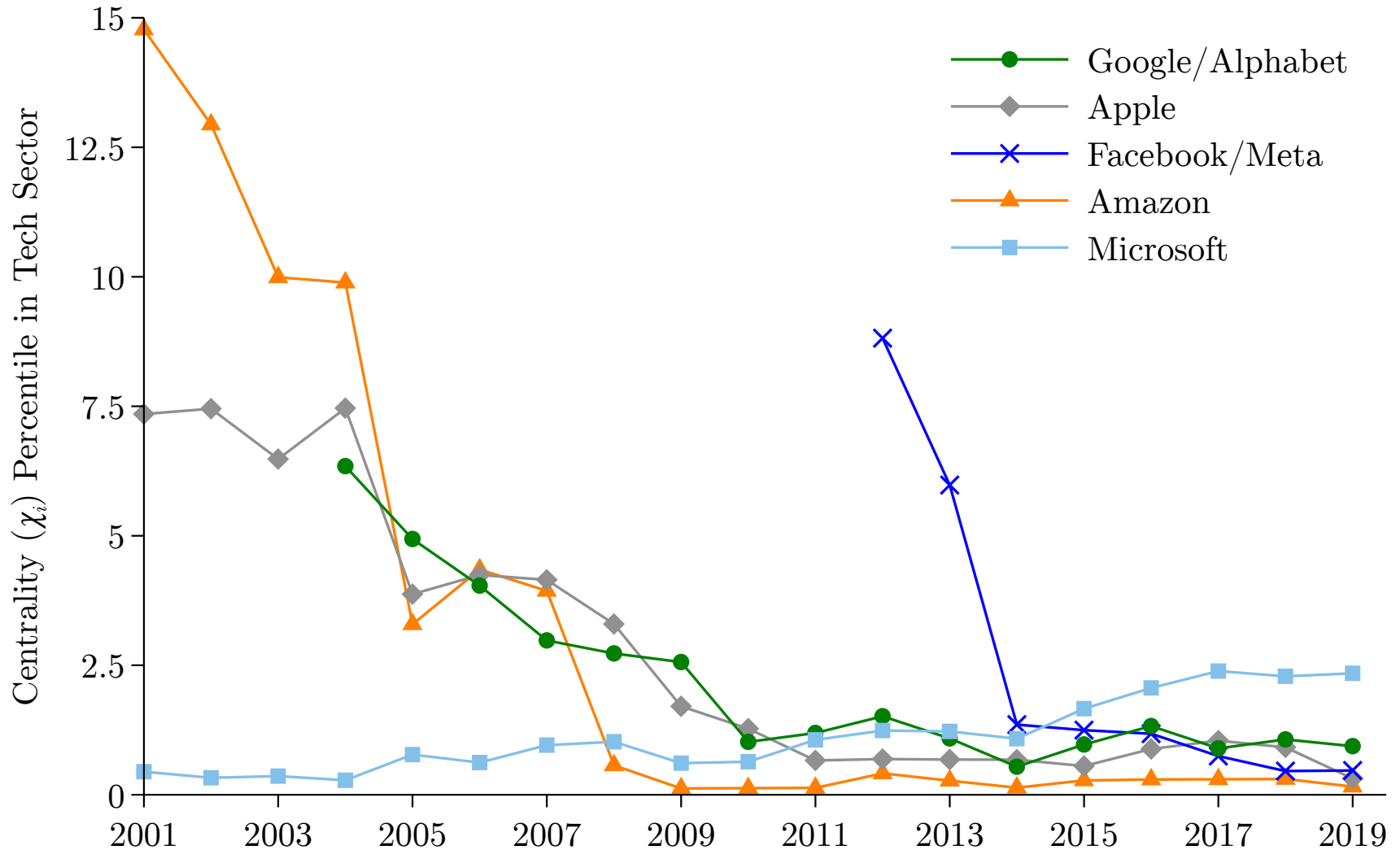
$$\text{EPP}_i = \frac{2q_i - \sqrt{f_i}}{b_i - c_i - 2q_i + \sqrt{f_i}}.$$



# Entrant Productivity Premium



# GAFAM Centrality



thank you